

# Cooperative Coevolutionary Invasive Weed Optimization and its Application to Nash Equilibrium Search in Electricity Markets



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## Philosophy

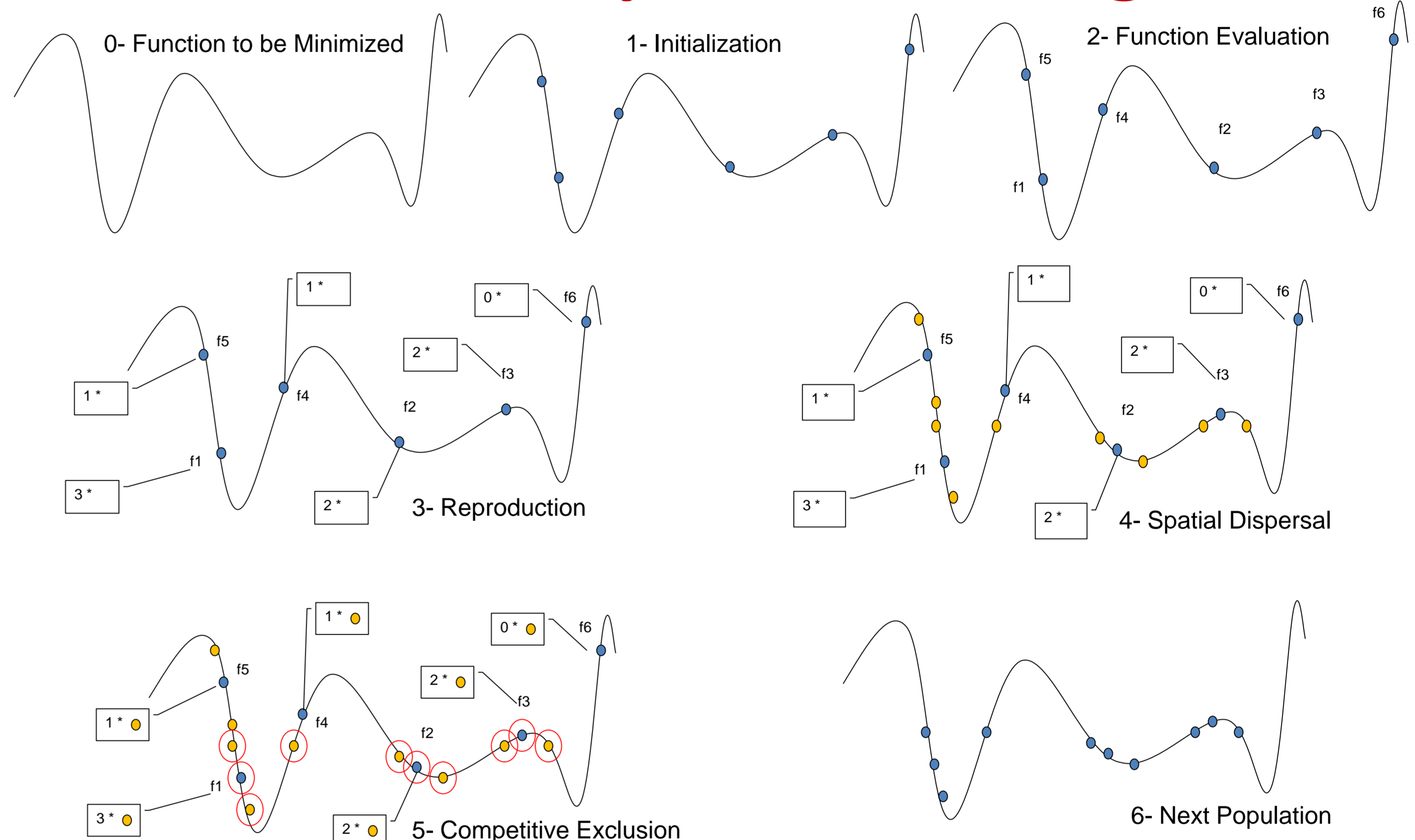
- Why Weeds?
  - The most robust and troublesome plant in agriculture.
  - After thousands of tillage and hand-weeding we still have weeds.
  - After 50 years of herbicides we still have weeds.
- Why Coevolutionary Computing:
  - Task decomposition
  - Parallel computation
  - Simulation of multiagent systems



## Motivation

- IWO improves search capability in Coevolutionary Algorithms
- Coevolutionary framework prepares a suitable basin for parallel computation and simulation of multiagent systems (like markets)

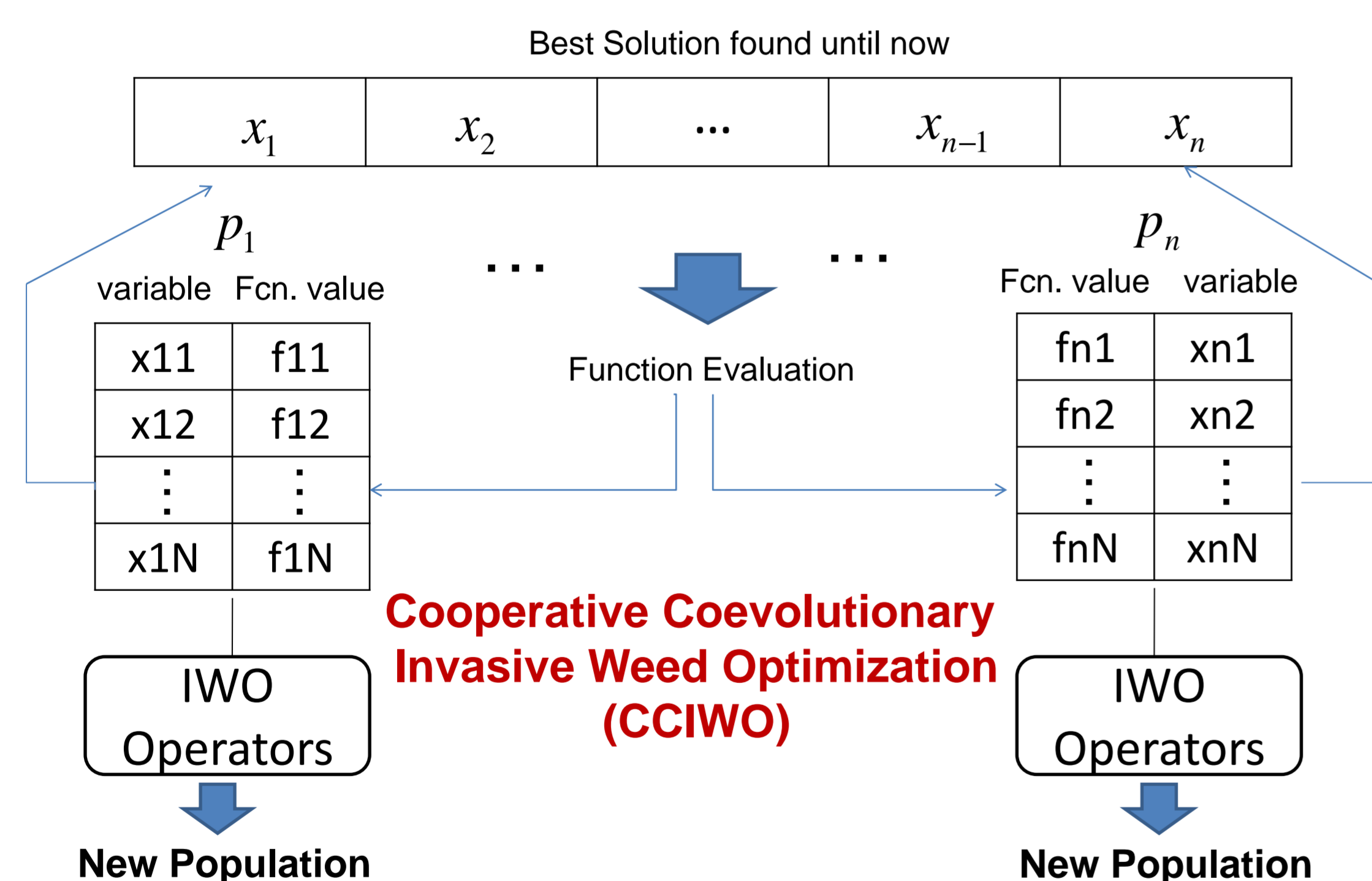
## Invasive Weed Optimization Algorithm



## Cooperative Coevolutionary Algorithm

- General Cooperative Coevolutionary Algorithm

1. For population  $p_s \in P$ , all populations
  - a. Initialize population  $p_s$ ;
2. For population  $p_s \in P$ , all populations
  - a. Evaluate population  $p_s$  with collaborators;
3. For  $t=0$  until a terminating criterion is met
  - a. For population  $p_s \in P$ , all populations
    - i. Evolutionary process to make next generation;
    - ii. Evaluate next generation with collaborators;
4. Next  $t$



## Results of CCIWO for Function Optimization

Name	Function	Initial range	Modality
Sphere	$\sum_{i=1}^n (x_i^2)$	[-100, 100]	unimodal
Rosenbrock	$\sum_{i=1}^n [100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2]$	[-2.12, 2.12]	unimodal
Rastrigin	$\sum_{i=1}^n (x_i^2 - 10 \cos(2\pi x_i) + 10)$	[-5.12, 5.12]	multimodal
Ackley	$-20 \exp(-0.2 \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2}) - \exp(\frac{1}{n} \sum_{i=1}^n \cos(2\pi x_i)) + 20 + e$	[-32, 32]	multimodal
Griewank	$1 + \sum_{i=1}^n (\frac{x_i^2}{4000}) - \prod_{i=1}^n \cos(\frac{x_i}{\sqrt{i}})$	[-600, 600]	multimodal

FUNCTION	Mean value			Number of Function Evaluation		
	CCGA	LCGA	CCIWO	CCGA	LCGA	CCIWO
Sphere	1e-08	1e-12	4e-13	600000	600000	326203
Rosenbrock	70	90	0.27	600000	600000	323635
Rastrigin	0.5	0.12	4e-10	600000	600000	324578
Ackley	0.8	8	3e-07	600000	600000	316616
Griewank	0.02	2	2e-12	600000	600000	323789

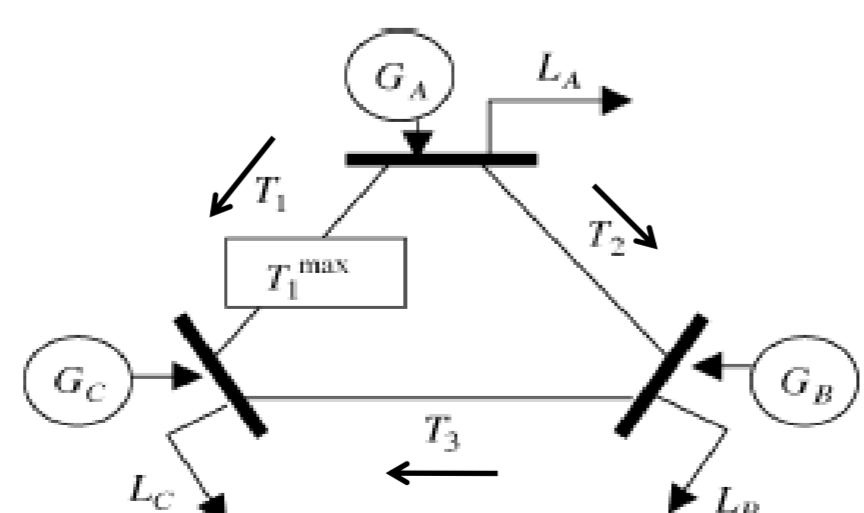
## Transmission-Constrained Electricity Markets

$$\max \left\{ P_i q_i - Cost_i \mid \max \sum_j Benefit_j \right. \\ \left. \text{St. Transmission Constraints} \right\}$$

$q_i$ : bidding strategy for producer  $i$   
 $P_i$ : local clearing price of market

- Three Bus Cournot Model with Linear Demand Function

$$\begin{aligned} B_1(d_1) &= -0.0555d_1^2 + 108.4096d_1 & C_1(q_1) &= 0.00786q_1^2 + 1.3606q_1 \\ B_2(d_2) &= -0.0669d_2^2 + 103.8238d_2 & C_1(q_1) &= 0.010526q_1^2 - 2.07807q_1 \\ B_3(d_3) &= -0.0637d_3^2 + 108.6709d_3 & C_1(q_1) &= 0.006478q_1^2 + 8.105354q_1 \end{aligned}$$



## Nash Equilibrium (NE)

$u_i$ : strategy for player  $i$       $\pi_i$ : payoff for player  $i$

$\{u_1^*, \dots, u_n^*\}$  is a Nash Equilibrium if :

$$\forall i, \forall u_i \quad \pi_i(u_1^*, \dots, u_i^*, u_{i+1}^*, \dots, u_n^*) \geq \pi_i(u_1^*, \dots, u_i, u_{i+1}^*, \dots, u_n^*)$$

## Results of NE Search with CCIWO

$$\pi_i = \lambda_i^* q_i - C_i(q_i)$$

where  $\lambda_i^*$  s are the lagrange multipliers of energy balance equality conditions in :

$$\max_d (B_1(d_1) + B_2(d_2) + B_3(d_3))$$

$$\text{S.T.} \quad q_1 - d_1 = 2T_1 - T_3, \quad q_2 - d_2 = -T_1 + 2T_3, \\ q_3 - d_3 = -T_1 - T_3, \quad |T_1| < T_1^{\max}$$

